

# Order toxicity and liquidity crisis: An academic point of view on Flash Crash

**Discussant**

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We review two papers on the causes of the Flash Crash by [Easley, De Prado and O'Hara](#):

- “The Microstructure of Flash Crash” (Working Paper November 2010)
- “Flow Toxicity and Volatility in High Frequency World” (Working Paper February 2011)

# Summary

- 1 Flash Crash caused by severe mismatch in liquidity: liquidity providers withdraw from the market or even turned into liquidity takers.
- 2 Liquidity dries up due to “toxic” (unbalanced) order flows.
- 3 Authors propose a measure of order toxicity, the VPIN metric.
- 4 They show that this VPIN measure anticipated the Flash Crash.

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# Recent trends in market structure

- Since 2009, HF trading firms ( $\approx 2\%$  of total 20,000 US firms) accounted for over 70% of U.S. equity trading volume.
- Many of these HF firms are in the business of “liquidity provision”, i.e. acting as market maker (MM) to “position takers”.
- HF MM generally do not make directional bets, but rather strive to earn razor thin margins on large numbers of trades.
- Their ability to do so depends on limiting their position risk by:
  - hold very small or zero inventory positions
  - have high inventory turnover (5 or more times a day)
  - control “adverse selection”
- $\Rightarrow$  Allow them to operate with very low capital, essentially using their speed of trading to control inventory risk.

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# Market Microstructure Models

- Microstructure models view trading as a game between liquidity providers (or MM) and liquidity takers (or traders or position takers).
- MMs set the spread to be compensated for:
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- Adverse selection arises because some traders may have better information on the future price than MM.
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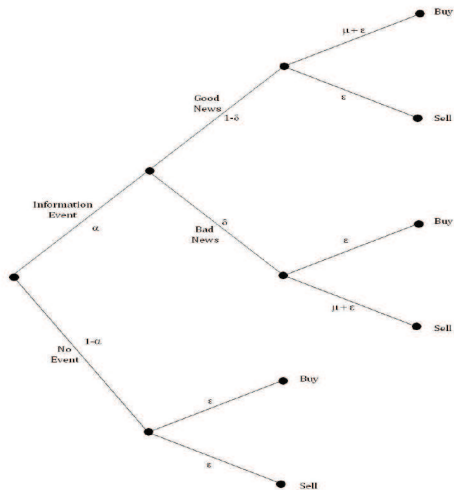
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# Sketch of a simple model of adverse selection





# Market Microstructure Models

- If  $\delta = 1/2$ , it can be shown that the bid-ask spread simplified to

$$s = \frac{\alpha\mu}{\alpha\mu + 2\epsilon} [\bar{S}_i - \underline{S}_i]$$

where  $\bar{S}_i$  and  $\underline{S}_i$  are price predictions of informed trades in case of good and bad news.

- The probability that a trade in a period is information-based (PIN) is

$$PIN = \frac{\alpha\mu}{\alpha\mu + 2\epsilon}$$

where  $\alpha\mu + 2\epsilon$  is the arrival rate for all orders and  $\alpha\mu$  is the arrival rate for information-based orders.

- PIN is thus a measure of the fraction of orders that arise from informed traders relative to the total order flow.
- MMs need to correctly estimate their PIN in order to identify the optimal spread  $s$ .

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# PIN estimation: VPIN theory

- Standard approach to estimate the PIN is to employ maximum likelihood estimation to get the unobservable parameters  $\alpha, \mu, \epsilon$  and then derive PIN from those estimates.
- The Authors propose a more direct volume-based approach observing that:

the expected trade imbalance is:

$$\mathbb{E} \left[ \left| V_{\tau}^S - V_{\tau}^B \right| \right] \approx \alpha \mu$$

where  $V_{\tau}^S$  is the sell volume and  $V_{\tau}^B$  is the buy volume.

and the expected arrival rate of total trades  $V = V_{\tau}^S + V_{\tau}^B$  is:

$$\mathbb{E} [V] = \alpha \mu + 2\epsilon$$

- Hence, the *Volume-Synchronized Probability of Informed Trading* VPIN is

$$PIN = \frac{\alpha \mu}{\alpha \mu + 2\epsilon} \approx \frac{\alpha \mu}{V} \approx \frac{\sum_{\tau=1}^n |V_{\tau}^S - V_{\tau}^B|}{nV} = VPIN$$

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# VPIN in practice

$$VPIN = \frac{\sum_{\tau=1}^n |V_{\tau}^S - V_{\tau}^B|}{nV}$$

- Sample the prices in “Volume-time”, i.e. in intervals having equal amount of volume  $V$ . They choose  $V = 1/50$  of the average daily volume and  $n = 50 \Rightarrow$  “daily” VPIN (on average).
- Volume Classification (in buy  $V_{\tau}^B$  and sell  $V_{\tau}^S$  volume).

Trade classification is always problematic: more so in the HF world of electronic order book where applying standard tick-based algos over individual transactions would be “futile”.

$\Rightarrow$  propose to aggregate trades over short time intervals  $\Delta$  (e.g. 1-minute) and sign the aggregated volume in that time interval as the corresponding transaction:

An aggregated transaction is buy if either

- i  $P_i > P_{i-\Delta}$  or
- ii  $P_i = P_{i-\Delta}$  and the transaction  $i - \Delta$  was also a buy.

Otherwise, the transaction is a sell.



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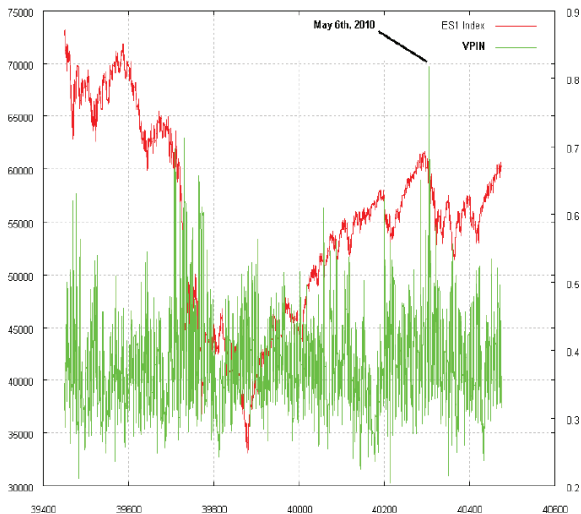
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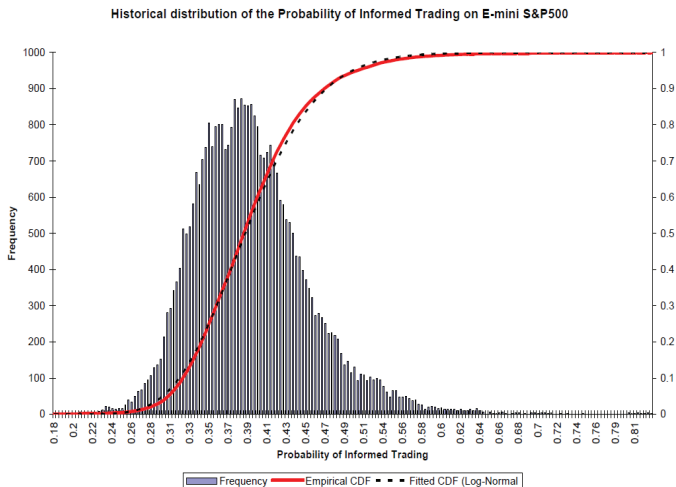
# VPIN of E-mini S&P500 over 3 years



:= 40142.3 y= 76009.0 y2= 0.920141

Figure 2 - VPIN metric between January 1<sup>st</sup> 2008 and October 30<sup>th</sup> 2010

# VPIN: Historical PDF and CDF



*Figure 3 - The empirical CDF of the VPIN metric as fitted through a log-normal distribution*

# VPIN 1 week before the Flash Crash

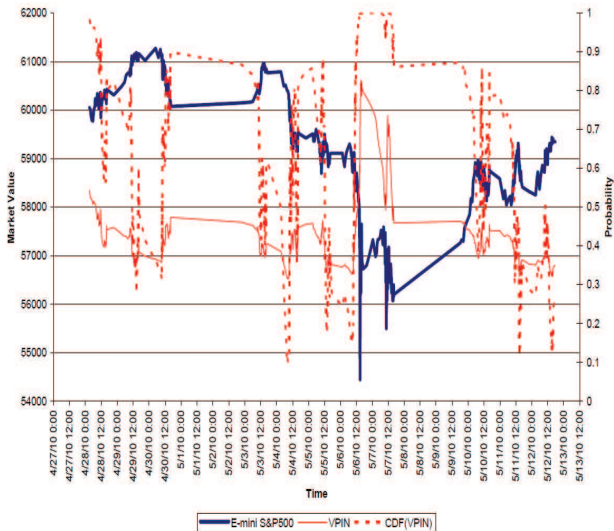


Figure 4 – E-mini S&P 500's VPIN metric one week before and after the flash crash

# VPIN on the Flash Crash day

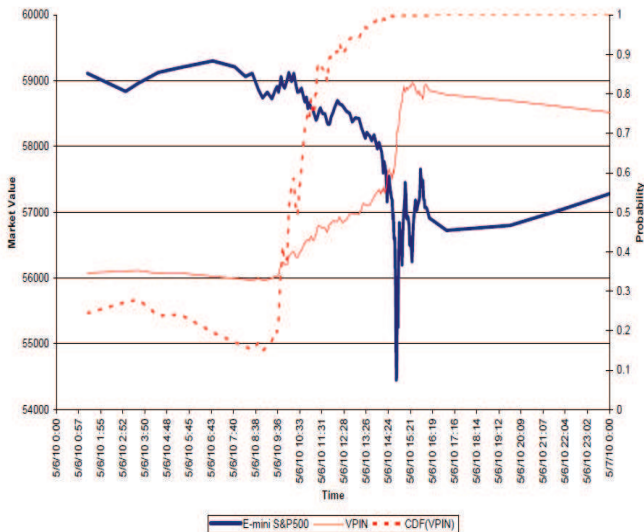


Figure 5 – E-mini S&P 500's VPIN metric on May 6<sup>th</sup>

# VPIN vs VIX

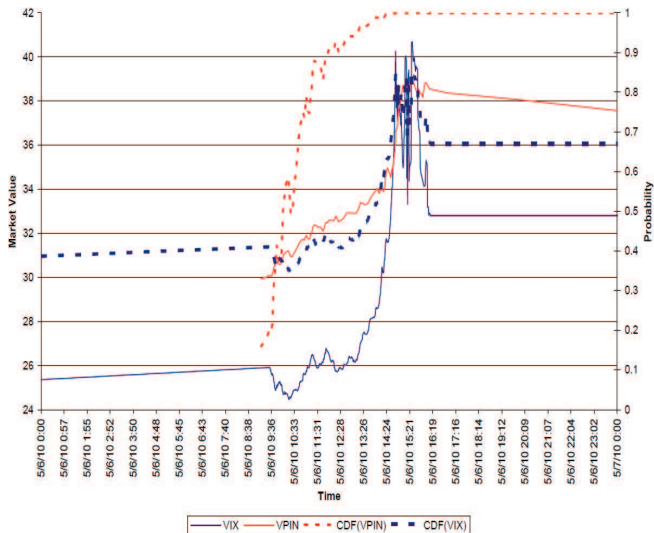


Figure 6 – VIX and E-mini's VPIN metric during the crash

# Point of caution: Impact trade aggregation interval

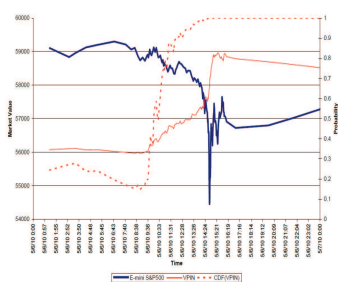


Figure 8(a) – VPIN estimated with One-Minute Time Bars

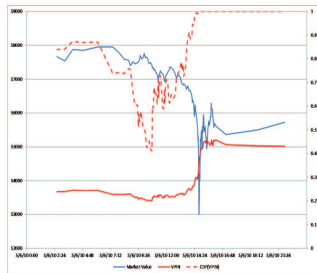


Figure 8(b) – VPIN Estimated with Ten-Second Time Bars

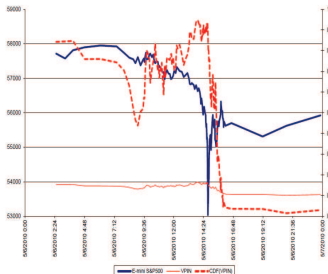


Figure 8(c) – VPIN Estimated with Trade-by-Trade Data

# VPIN of EUR/USD and T-Note

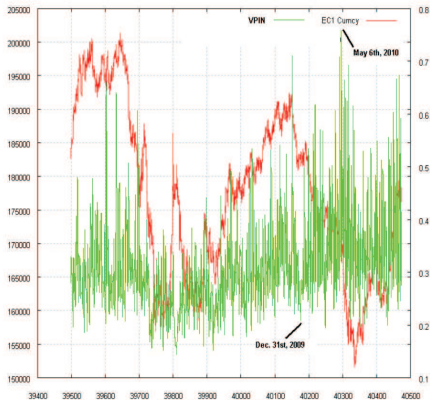


Figure 10 - VPIN for EUR/USD futures

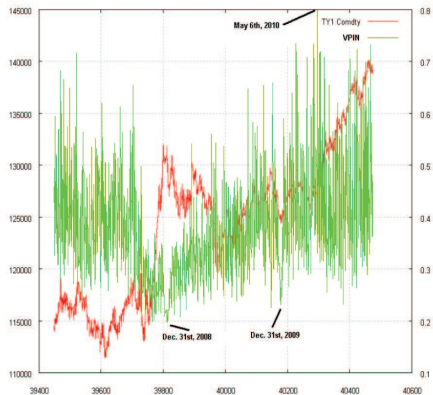


Figure 11 - VPIN for T-Note futures



# Conclusions

- Flash Crash causes:
  - When flow toxicity unexpectedly rose (unusually unbalanced order flow as measured by VPIN) HF MMs face large losses.
  - Inventory may grow beyond their risk limits, forcing them to withdraw from the market.
  - If they keep accumulating losses, at some point they may capitulate, dumping their inventory to take the loss.

Hence, extreme toxicity can transform liquidity providers into liquidity consumers.

- By measuring imbalance in order flow (toxicity) the proposed **VPIN metric should predict liquidity crisis** (as claimed for the Flash Crash).
- Authors **proposed solution to liquidity crisis**: Creating an exchange future with the VPIN metric as underlying.